

8-4: MULTIPLYING SPECIAL CASES

Lesson Objectives:

- Finding the square of a binomial
- Finding the difference of two squares

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Finding the Square of a Binomial

The expressions $(a + b)^2$ and $(a - b)^2$ are squares of binomials. To square a binomial, you can use FOIL or the following shortcut.

RULE: THE SQUARE OF A BINOMIAL

and

The square of a binomial is the square of the first term, plus twice the product of the two terms, plus the square of the last term.

EXAMPLE 1: SQUARRING A BINOMIAL

Simplify.

1. $(x + 4)^2$

2. $(y - 3)^2$

3. $(y + 11)^2$

4. $(3w - 5)^2$

5. $(t + 6)^2$

6. $(x - 7)^2$

7. $(9c - 8)^2$

8. $(3m + 2n)^2$

9. $(x^2 + y^2)^2$

10. $(2x^2 + y^2)^2$

11. $(y^2 - 4w^2)^2$

12. $(5x^4 - 3x^2)^2$

EXAMPLE 2: MENTAL MATH

Simplify in your mind.

13. 81^2

14. 59^2

15. 31^2

16. 29^2

17. 98^2

18. 203^2

2 Difference of Squares

The product of the sum and difference of the same two terms also produces a pattern.

RULE: THE DIFFERENCE OF TWO SQUARES

$$(a + b)(a - b) =$$

The product of the sum and difference of the same two terms is the difference of their squares.

EXAMPLE 3: FINDING THE DIFFERENCE OF TWO SQUARES

Simplify.

19. $(x + 4)(x - 4)$

20. $(3x - 5)(3x + 5)$

21. $(p^4 - 8)(p^4 + 8)$

22. $(d + 11)(d - 11)$

23. $(c^2 + 8)(c^2 - 8)$

24. $(9v^3 + w^4)(9v^3 - w^4)$

25. $(x^2 - 2y)(x^2 + 2y)$

26. $(3x + 4)(3x + 4)$

EXAMPLE 4: MENTAL MATH

Simplify in your brains.

27. $(18)(22)$

28. $(19)(21)$

29. $(59)(61)$

30. $(87)(93)$

31. $(96)(104)$

32. $(33)(47)$

33. Find the area of the shaded region that is (eventually) drawn on the board.

34. Simplify.

a) $(x+4)(x+3)$

b) $(x+4)(x-4)$

c) $(x-4)^2$

d) $(2x-7)(2x+7)$

e) $(2x-1)(2x+3)$

f) $(2x+5)^2$

Name _____

8-4 Practice Worksheet

Period _____

Simplify each product.

1. $(x+4)^2$

2. $(3m+7)^2$

3. $(b-5)^2$

4. $(9j-2)^2$

5. $(a+8)(a-8)$

6. $(h+15)(h-15)$

7. $(k+5)(k-5)$

8. $(x-7y)^2$

9. $(6a+11b)^2$
 $(g^3-7h^2)(g^3+7h^2)$

10. $(y^5-9x^4)^2$

11. $(2d+7g)(2d-7g)$

12.

Use mental math to find each product. Show the setup step.

13. 302^2

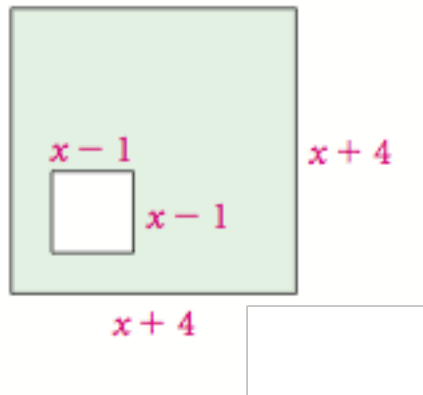
14. 499^2

15. $(197)(203)$

16. $(299)(301)$

Find an expression for the area of the shaded region.

17. $A_{\text{square}} = (\text{length of a side})^2$

**MIXED REVIEW****Evaluate each expression for $x=3$, $y=-1$, and $z=2$.**

18. $-xyz$

19. $-z^3 - 2z + z$

20. $y^2 - (-y)^2$

Suppose you have a bag containing 3 red, 4 blue, 5 white, and 2 black marbles. You select one marble at random. Find each probability or odds.

21. $P(\text{not white})$ 22. $P(\text{red or blue})$ 23. $P(\text{orange})$ 24. $P(\text{not black})$

25. odds in favor of red 26. odds against blue 27. odds against black or white

28. odds in favor of red, white, or blue

You have 8 red checkers and 8 black checkers in a bag. You choose two checkers. Find each probability.

29. $P(\text{red and red})$ with replacing

30. $P(\text{red then black})$ without replacing

31. $P(\text{black and red})$ with replacing